

Factor the following COMPLETELY

1. $x^2 - 81$ **DOS**

$(x+9)(x-9)$

2. $x^2 - 11x + 18$ **a=1**

$$\begin{array}{c} \begin{array}{ccc} & 18 & \\ -9 & \times & -2 \\ & -11 & \end{array} \\ -9 \cdot -2 = 18 \\ -9 + -2 = -11 \end{array}$$

$(x-9)(x-2)$

3. $2x^2 - 7x - 4$ **a>1**

$$\begin{array}{c} \begin{array}{ccc} & -8 & \\ -8 & \times & 1 \\ & -7 & \end{array} \\ -8 \cdot 1 = -8 \\ -8 + 1 = -7 \end{array}$$

$2x^2 + 1x - 8x - 4$
 $x(2x+1) - 4(2x+1)$
 $(2x+1)(x-4)$

4. $8x^2 + 24$ **GCF**

$8(x^2 + 3)$

5. $4x^2 - 49$ **DOS**

$(2x+7)(2x-7)$

6. $x^2 - x - 20$ **a=1**

$$\begin{array}{c} \begin{array}{ccc} & -20 & \\ -5 & \times & 4 \\ & -1 & \end{array} \\ -5 \cdot 4 = -20 \\ -5 + 4 = -1 \end{array}$$

$(x-5)(x+4)$

7. $5x^2 + 25x + 30$

$5(x^2 + 5x + 6)$ **GCF, a=1**

$$\begin{array}{c} \begin{array}{ccc} & 6 & \\ 3 & \times & 2 \\ & 5 & \end{array} \\ 3 \cdot 2 = 6 \\ 3 + 2 = 5 \end{array}$$

$5(x+3)(x+2)$

8. $-3x^2 + 9$ **GCF**

$-3(x^2 - 3)$

9. $4x^2 - x - 5$ **a>1**

$$\begin{array}{c} \begin{array}{ccc} & -20 & \\ 4 & \times & -5 \\ & -1 & \end{array} \\ 4 \cdot -5 = -20 \\ 4 + -5 = -1 \end{array}$$

$4x^2 + 4x - 5x - 5$
 $4x(x+1) - 5(x+1)$
 $(4x-5)(x+1)$

10. $3x^2 - 9x - 30$

$3(x^2 - 3x - 10)$ **GCF**

$$\begin{array}{c} \begin{array}{ccc} & -10 & \\ -5 & \times & 2 \\ & -3 & \end{array} \\ -5 \cdot 2 = -10 \\ -5 + 2 = -3 \end{array}$$

$3(x-5)(x+2)$ **a=1**

11. $x^2 + 8xy + 12y^2$

$$\begin{array}{c} \begin{array}{ccc} & 12 & \\ 6 & \times & 2 \\ & 8 & \end{array} \\ 6 \cdot 2 = 12 \\ 6 + 2 = 8 \end{array}$$

$(x+6y)(x+2y)$ **a=1**

12. $12x^2 - 15x$

$3x(4x-5)$ **GCF**

Plot all the points from your table that fit on the graph and sketch your parabola:

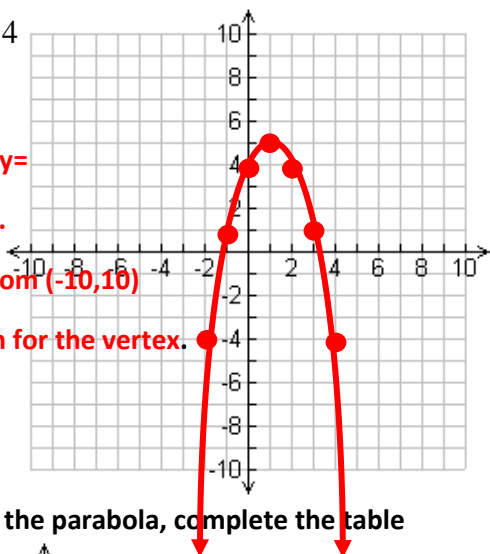
13. $y = -x^2 + 2x + 4$

Put the equation in $y=$

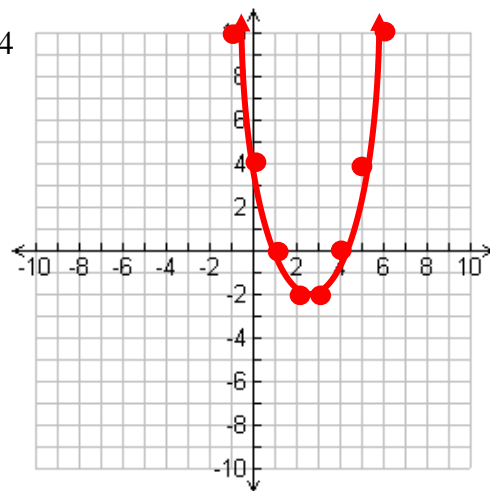
Then go to 2nd table.

Plot all the points from $(-10,10)$

use the trace button for the vertex.

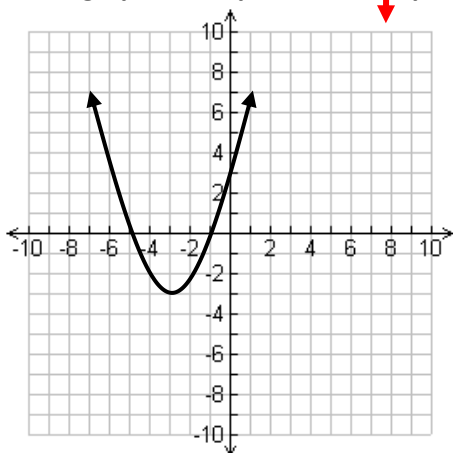


14. $y = x^2 - 5x + 4$



Given the graph of the parabola, complete the table

15.



x-intercepts:

$(-5,0)(-1,0)$

y-intercept:

$(0,3)$

Domain:

\mathbb{R}

Range:

$[-3, \infty)$

Increasing:

$(-3, \infty)$

Decreasing:

$(-\infty, -3)$

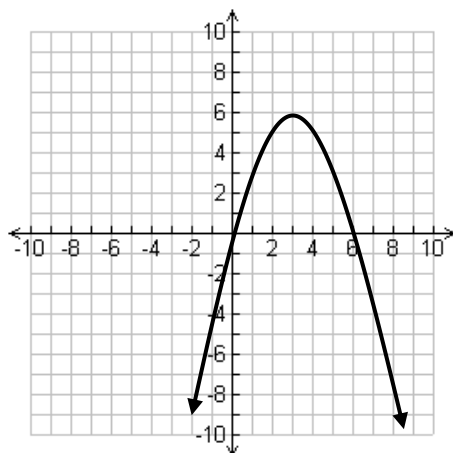
As $x \rightarrow \infty, f(x) \rightarrow$

∞

As $x \rightarrow -\infty, f(x) \rightarrow$

∞

16.



x-intercepts:

$(0,0)(6,0)$

y-intercept:

$(0,0)$

Domain:

\mathbb{R}

Range:

$(-\infty, 6)$

Increasing:

$(-\infty, 3)$

Decreasing:

$(3, \infty)$

As $x \rightarrow \infty, f(x) \rightarrow$

$-\infty$

As $x \rightarrow -\infty, f(x) \rightarrow$

$-\infty$

Solve each equation algebraically: factoring or quadratic formula

17. $2x^2 + 14x = 0$
 $2x(x+7) = 0$ factor GCF
 $2x = 0, x+7 = 0$ set =0
 $x = 0, x = -7$

18. $3x^2 - 8 = -2x$
 $3x^2 + 2x - 8 = 0$ standard form
 $\begin{array}{r} -24 \\ 6 \times -4 \\ \hline 2 \end{array}$
 $6 \cdot -4 = -24$
 $6 + -4 = 2$
 $3x^2 + 6x - 4x - 8 = 0$
 $(3x-4)(x+2) = 0$ factor a>1
 $3x-4 = 0, x+2 = 0$ set =0
 $x = 4/3, x = -2$

19. $x^2 - 11x + 18 = 0$
 $\begin{array}{r} 18 \\ -2 \times -9 \\ \hline -11 \end{array}$
 $-2 \cdot -9 = 18$
 $-2 + -9 = -11$
 $(x-2)(x-9) = 0$ factor a=1
 $x-2 = 0, x-9 = 0$ set =0
 $x = 2, x = 9$

20. $3x + 4 = -x^2$
 $x^2 + 3x + 4 = 0$ standard form
 $x = \frac{-3 \pm \sqrt{3^2 - 4 \cdot 1 \cdot 4}}{2 \cdot 1}$ Q. Formula
 $x = \frac{-3 \pm \sqrt{9-16}}{2}$
 $x = \frac{-3 \pm \sqrt{-7}}{2}$
 $x = \frac{-3 \pm \sqrt{7}i}{2}$ $\sqrt{-1} = i$

21. $x^2 + 6x = -11$
 $x^2 + 6x + 11 = 0$ standard form
 $x = \frac{-6 \pm \sqrt{6^2 - 4 \cdot 1 \cdot 11}}{2 \cdot 1}$
 $x = \frac{-6 \pm \sqrt{36-44}}{2}$
 $x = \frac{-6 \pm \sqrt{-8}}{2} = \frac{-6 \pm \sqrt{8}i}{2}$
 $x = \frac{-6 \pm 2\sqrt{2}i}{2} = -3 \pm \sqrt{2}i$

22. $x^2 - 3x = 9$
 $x^2 - 3x - 9 = 0$ standard form
 $x = \frac{-(-3) \pm \sqrt{(-3)^2 - 4 \cdot 1 \cdot (-9)}}{2 \cdot 1}$
 $x = \frac{3 \pm \sqrt{9+36}}{2}$
 $x = \frac{3 \pm \sqrt{45}}{2}$
 $x = \frac{3 \pm 3\sqrt{5}}{2}$

Answer Explanations

Below are some QR codes that link to tutorial videos that you can reference to help you complete these problems.

Question #1,#5
factoring Difference of
squares



#2, #6, #11
trinomial a=1



#4,#8, #12
GCF



#3,#9
Trinomial a>1



#7,#10
GCF, Trinomial a=1



#13,14

1. Put the equation in y=
2. Click on 2nd table.
3. Plot all the points from (-10,10)
4. use the trace button for the vertex

#15,16

x-intercepts are the two points touching the x-axis. They should have 0 for the y-value. (,0), (,0)

y-intercept is the point touching the y-axis. It should have 0 for the x-value. (0,)

domain is all real numbers R

Range is the y-values from bottom to up

Increasing,decreasing are the x-values from left to right.

As $x \rightarrow \infty$ means the graph goes to the right side, then $f(x) \rightarrow$ put $-\infty$ for DOWN / ∞ for UP

As $x \rightarrow -\infty$ means the graph goes to the left side, then $f(x) \rightarrow$ put $-\infty$ for DOWN / ∞ for UP

#17-19

Solving quadratic equations by factoring




#20-23

When the quadratic function is not factorable, solve it using the quadratic equation. Remember, you need to put the equation in the standard form first.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

when $ax^2 + bx + c = 0$



#21.

- how to simplify the radical $\sqrt{8} = 2\sqrt{2}$?

Option 1. Use a calculator. Put $y=8/x^2$. Then go to the table and y value of 1. Then go up in the table and find the values that make both X and Y1 integers(without decimals). If you see 2 and 2 then it's $2\sqrt{2}$.

The image shows two parts of a calculator screen. On the left, the equation editor shows $Y_1 = 8/X^2$ and $Y_2 =$, $Y_3 =$, $Y_4 =$, and $Y_5 =$. On the right, the table function is displayed with columns X and Y1. The table contains the following values:

X	Y1
2	.88889
3	.5
4	.32
5	.22222
6	.16327
8	.125

At the bottom of the table screen, it says "Press + for Δtbl".

Option 2. Use the factor tree $8=2 \times 2 \times 2$. There's a pair of 2 that can come out of the radical as a 2. The other 2 stays inside the radical. $\sqrt{8} = \sqrt{2 \cdot 2 \cdot 2} = 2\sqrt{2}$

Or $\sqrt{8} = \sqrt{4 \cdot 2} = \sqrt{4}\sqrt{2} = 2\sqrt{2}$

- How to simplify $\frac{-6 \pm 2\sqrt{2}i}{2} = -3 \pm \sqrt{2}i$?

$$\frac{-6 \pm 2\sqrt{2}i}{2} = \frac{-6}{2} \pm \frac{2\sqrt{2}i}{2} = -3 \pm \sqrt{2}i$$

#22.

- how to simplify the radical $\frac{3 \pm \sqrt{45}}{2} = \frac{3 \pm 3\sqrt{5}}{2}$?

Option 1. Use a calculator. Put $y=45/x^2$. Then go to the table and y value of 1. Then go up in the table and find the values that make both X and Y1 integers(without decimals). If you see 3 and 5 then it's $3\sqrt{5}$.

The image shows two parts of a calculator screen. On the left, the equation editor shows $Y_1 = 45/X^2$ and $Y_2 =$, $Y_3 =$, $Y_4 =$, and $Y_5 =$. On the right, the table function is displayed with columns X and Y1. The table contains the following values:

X	Y1
2	11.25
3	5
4	2.8125
5	1.8
6	1.25
7	.91837
8	.70313

At the bottom of the table screen, it says "X=3".

Option 2. Use the factor tree $45=5 \times 3 \times 3$. There's a pair of 3 that can come out of the radical as a 3. 5 stays inside the radical. $\sqrt{45} = \sqrt{5 \cdot 3 \cdot 3} = 3\sqrt{5}$

Or $\sqrt{45} = \sqrt{9 \cdot 5} = \sqrt{9}\sqrt{5} = 3\sqrt{5}$